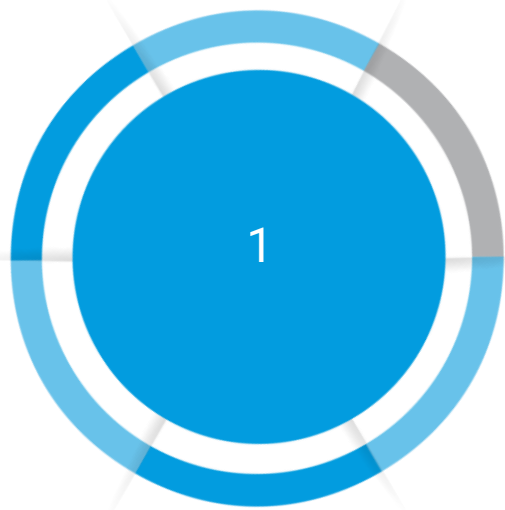


Bianca Wex, bianca.wex@lcm.at

# AC Losses and Transient Voltage Effects in Electric Machines

Efficient Simulation Methods

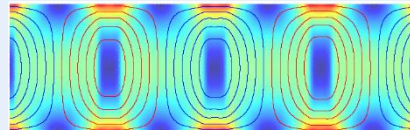
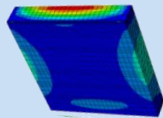
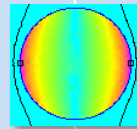


## AC Losses and Simulation Methods

# Overview of Additional Losses

Efficient simulation method

Based on magnetostatic FEM $f \leq f_{el} \frac{n_{Steps}}{2}$	Based on AC simulation with frozen permeability
Proximity and skin losses	Proximity and skin losses
Losses in parallel wires	
Magnet losses (slot harmonics, current distortion)	Magnetic losses due to PWM
Losses in rotating and stationary thin-walled sleeves	
	Losses in solid materials

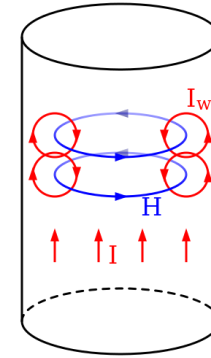


# Skin and proximity losses

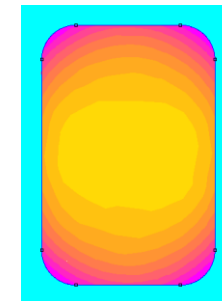
## Losses due to skin effect

- Background
  - Alternating current in the conductor generates a magnetic field, which causes an electric field induced in the conductor.
  - Current density in the middle of the conductor is reduced and at the outer boundary increased.
- Calculation method
  - Increase of resistance as a function of frequency  $K_e$
  - Analytical formula for round wire exists.
  - For conductors with arbitrary cross-sections  $K_e$  is calculated with FEA.

$$P_{skin} = m (K_e(f) - 1) R_{dc} I^2$$



Source: Wikipedia



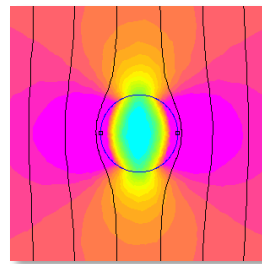
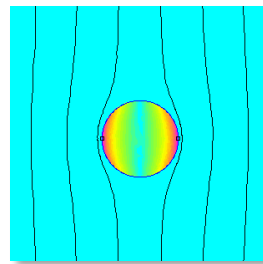
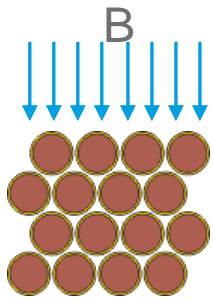
Current distribution in rectangular wire

# Skin and proximity losses

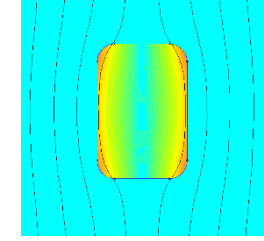
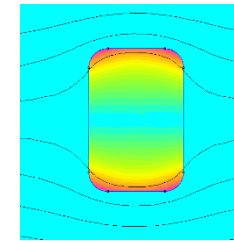
## Proximity losses

- Background
  - Losses due to the alternating magnetic fields, e.g. caused by leakage flux in the slots.
- Calculation method
  - Fourier spectrum of flux density is calculated with FEA for each conductor in slot.
  - Losses in the wire are calculated by means of a loss function  $F_p$

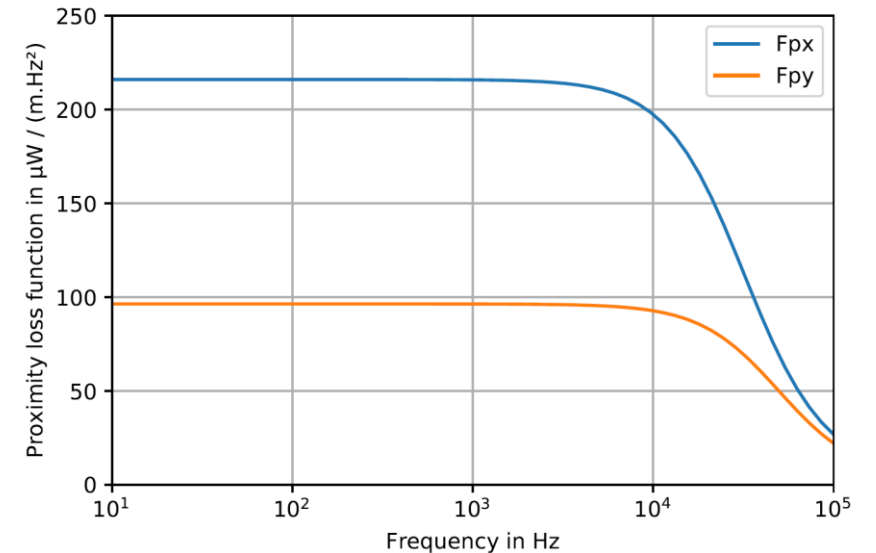
$$P_{prox} = \sum_{N_s} \sum_{n_c} \sum_{\nu} (F_{px} B_{x\nu}^2 + F_{py} B_{y\nu}^2) f_1^2 l \nu^2$$



Flux density and current density distribution



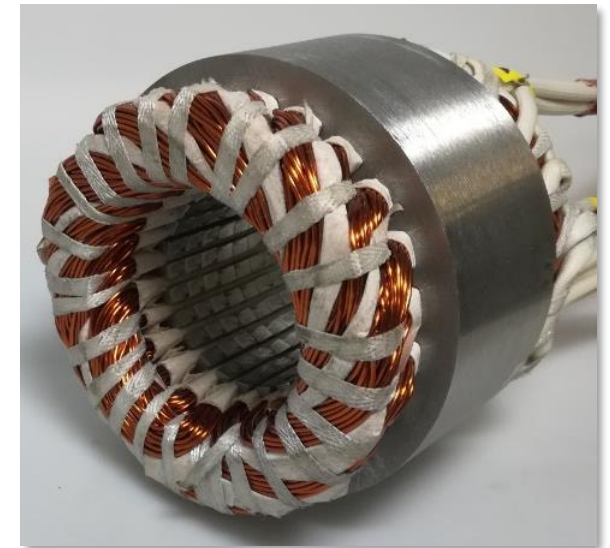
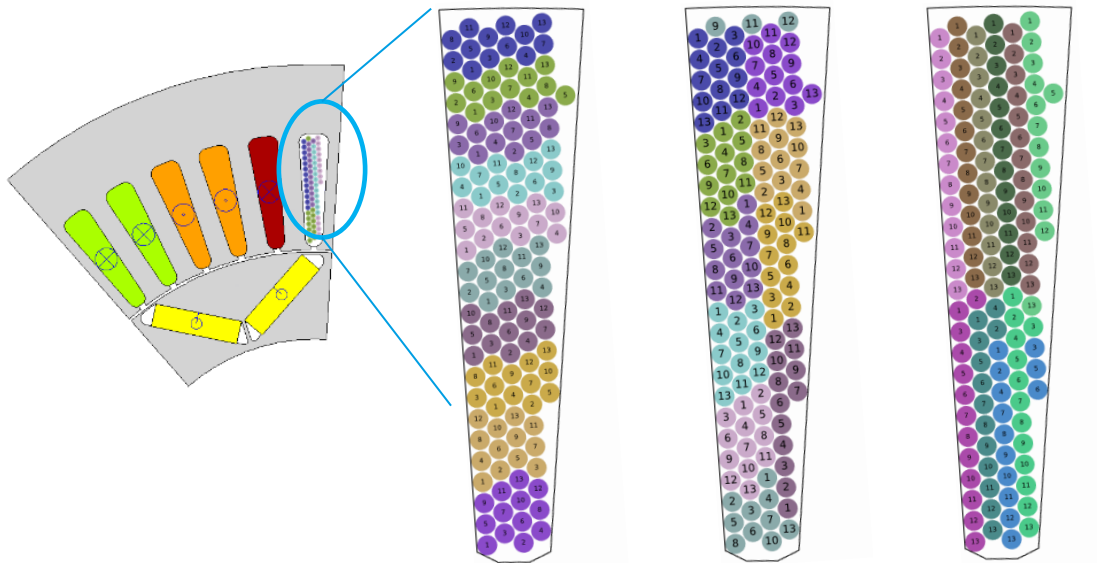
$$F_{px} = \frac{P_{px}}{f^2 B_x^2 l} \quad F_{py} = \frac{P_{py}}{f^2 B_y^2 l}$$



# Losses in stranded windings

## Background

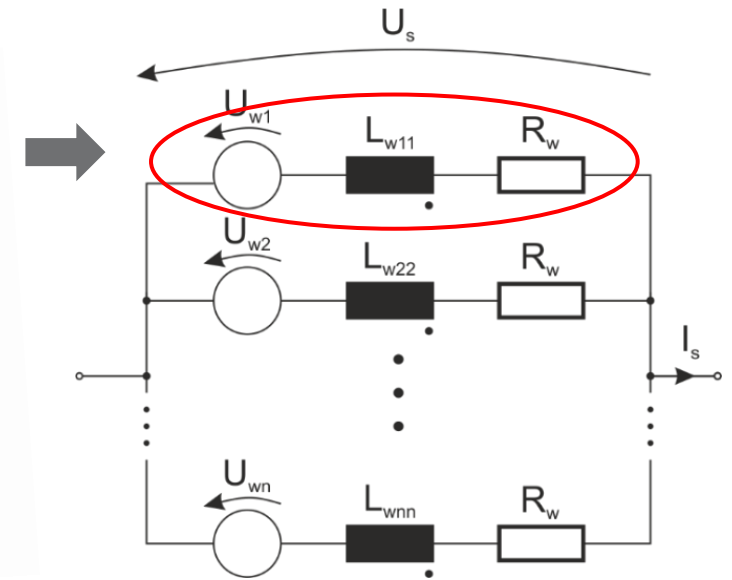
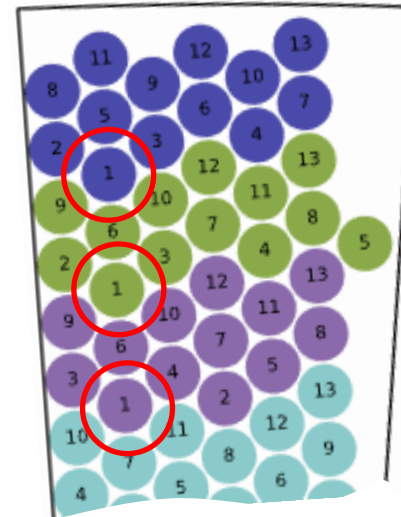
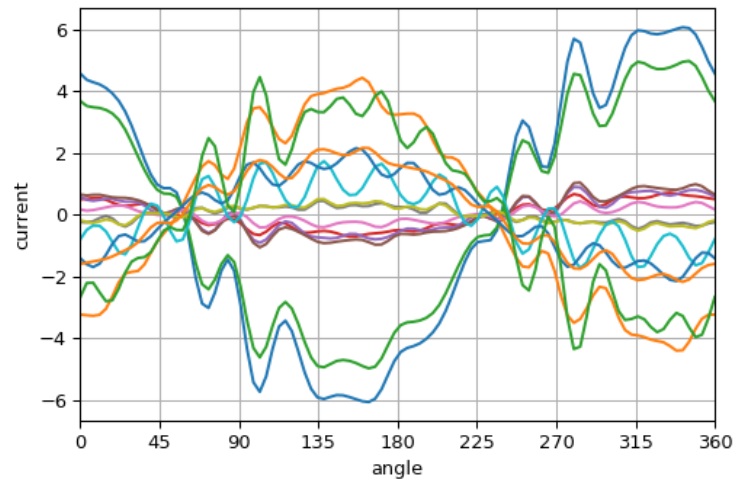
- Power density of electrical machines increases with speed.
- The number of turns decreases, and the wire cross-section increases with increasing speed.
- At low turn count, winding conductors are often subdivided into multiple insulated strands.
- The arrangement of the wires in the slot depends on the manufacturing process.



# Losses in stranded windings

## Calculation method

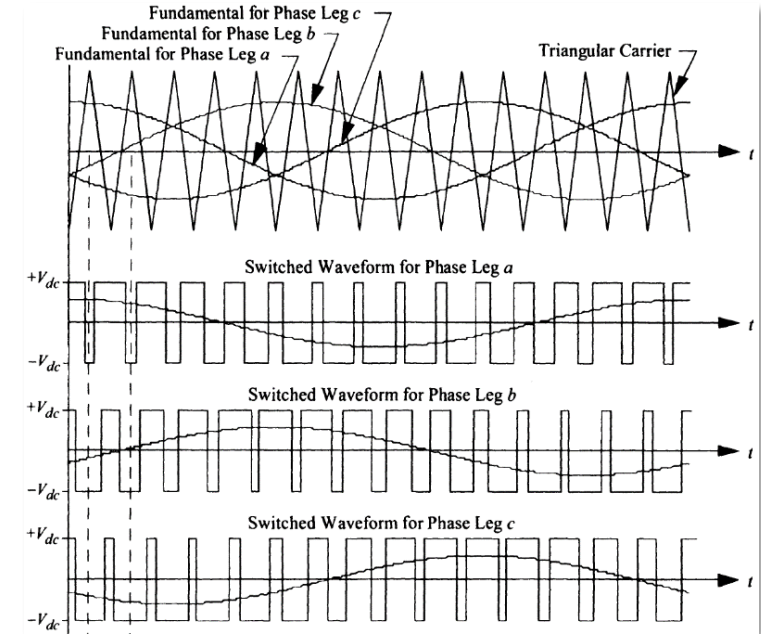
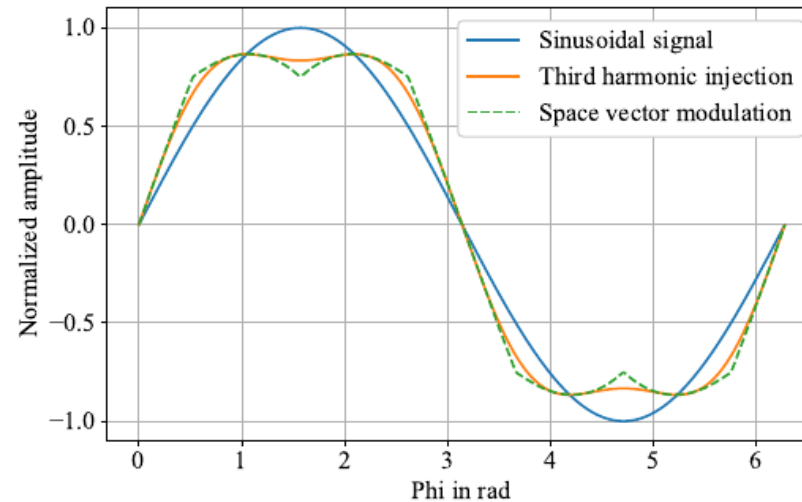
- Parameters of the equivalent circuit are calculated with FEA in the frequency domain
- Circulating currents and additional copper losses are evaluated



# Losses due to PWM Harmonics

## Calculation of PWM signal

- Calculation is carried out in the frequency domain.
- Intersection of modulated voltage with triangular carrier.
- Calculation of the Fourier coefficients for each switching cycle of the voltage signal for
  - Third harmonic injection
  - Space vector modulation
  - Discontinuous PWM min
  - Discontinuous PWM max
  - 2- or 3-level PWM

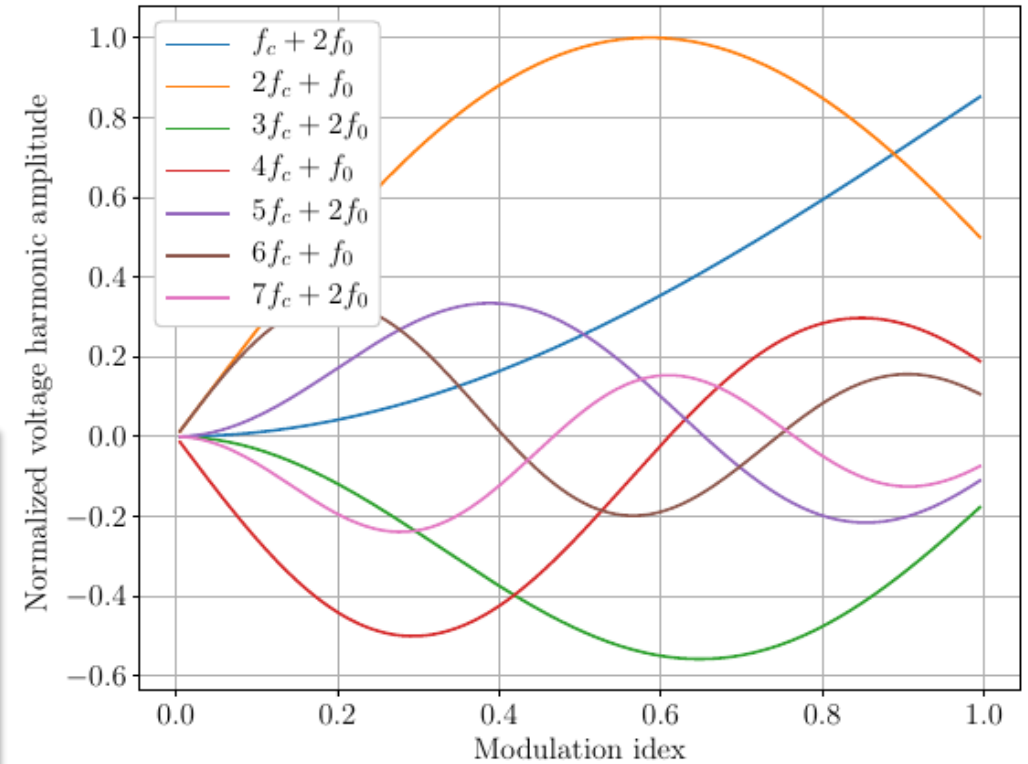
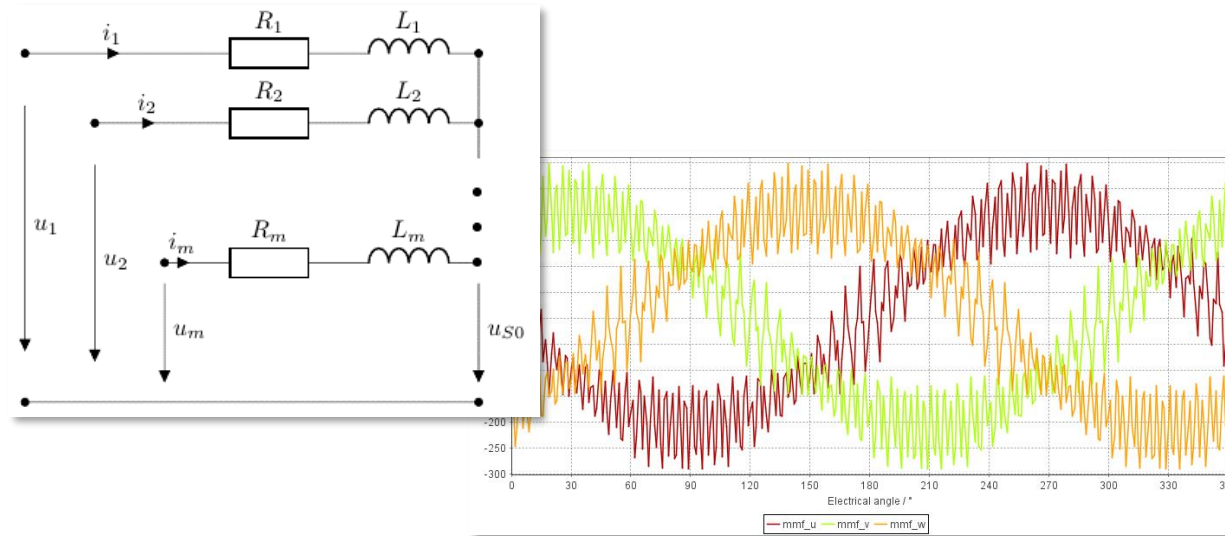




# Losses due to PWM Harmonics

## Calculation of PWM signal

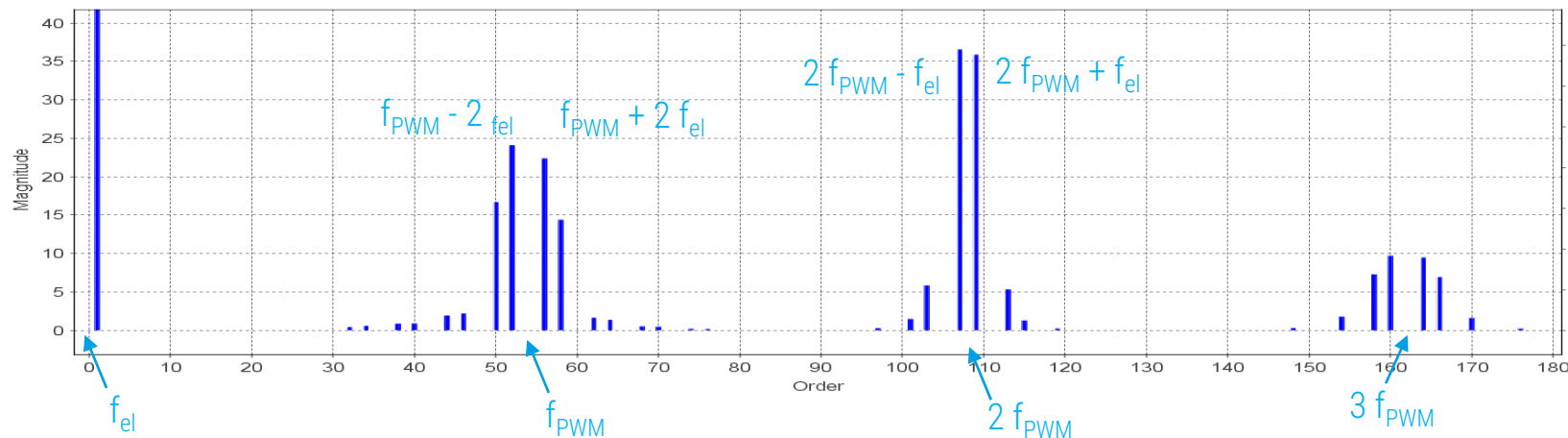
- Evaluation of the currents for a symmetrical m phase system with floating star connection.
- Frequency dependent inductances and resistances are used for current calculation.

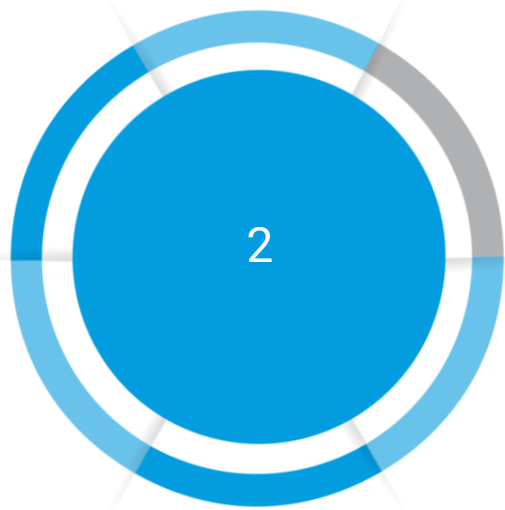


# Losses due to PWM Harmonics

## Loss calculation

- Simulation of the permeability distribution in the laminated core for the considered load point.
- Calculation of losses as a function of frequency with AC FE Solver at "frozen" permeabilities.
- Evaluation of losses in solid and laminated components.
  - Wire and hair pins
  - Laminated stack
  - Magnet





## AC losses – Loadpoint and dq Grid

Usage in SyMSpace

# AC losses in dq Grid in SyMSpace

## Add AC losses to WebGUI project

- Add Component „PMSM AClosses FEMM“ to PMSM Simulation
- Settings in Geometry.Stator.Coil:
  - *EnableACLoss* is set automatically to true after inserting AClosses
  - Set *wc*, *ncw*, *WireGrade* and *AspectFactor*
  - Check Preview of WireDiameter
- Further checks:
  - Preview of PMSM\_Model (check if the wires are drawn in the correct slots, especially for double layer windings)
  - Check if all materials have a field *rho\_el* or *kappa\_20*
  - Check if laminated materials have a field *tlam*

Wire

Previews

Winding Placement

Turn Grouping

Parameters

wc	Number of turns per coil	5.0	↻ 📄 ✎
ncw	Number of parallel wires per coil	13.0	↻ 📄 ✎
kcu_max	Maximum possible copper fill factor for coil	0.5	↻ 📄 ✎
WireGrade	Wire grade	'Grade2'	↻ 📄 ✎
Theta_c	Temperature of coil	120.0 degC	↻ 📄 ✎
lambda	Thermal conductivity for coil	0.8 W.m-1.K-1	↻ 📄 ✎
EnableACLoss	Enable AC loss calculation	true	↻ 📄 ✎
AspectFactor	Wire distribution factor (highest losses occur when the asp	0.85	↻ 📄 ✎

# AC losses in dq Grid in SyMSpace

## Postprocessing - PWM Settings

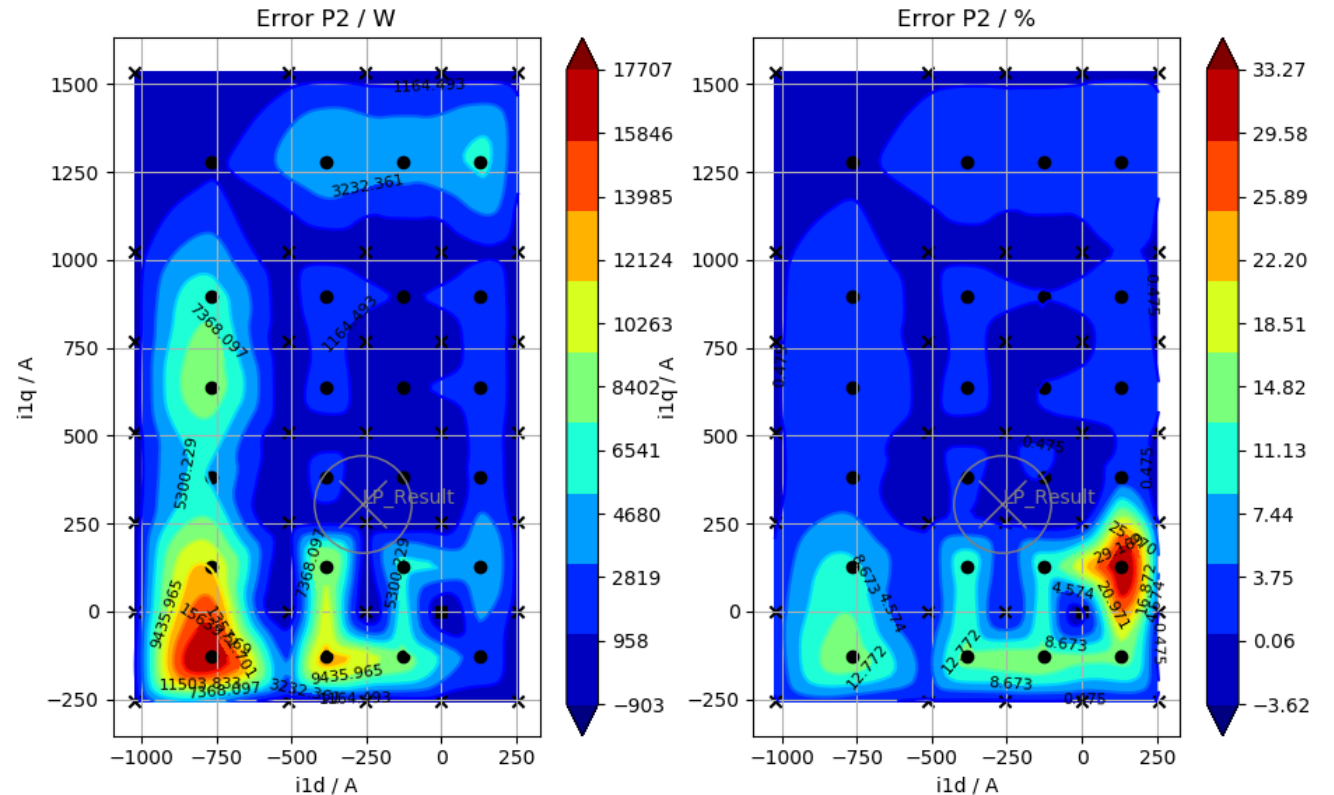
- Usage in Postprocessing (RBF) Components
  - AC losses are automatically evaluated according to settings in Postprocessing\_Settings
- Master PWM Settings in Postprocessing\_Settings.Power\_Supply
  - Constant PWM frequency or speed-dependent vector
  - *enable\_PWM*: default is false → set to true
  - *ModulationType*: sine, space vector, third harmonic, DPWM min, DPWM max
  - *InverterLevels*: 2 or 3
  - *MaxLossError*: default is 6 %, maximum order of PWM harmonics is automatically calculated from *MaxLossError*



# AC losses in dq Grid in SyMSpace

## Verification of Interpolation Quality

- First: check quality of load point interpolation
  - Add PMSM\_Model\_Verification\_FEMM component to your project
  - In general (also for basic models without AC losses) highly recommended
- Check interpolated AC loss results
  - Add a PMSM\_Loadpoint\_AClosses\_FEMM component to your project and link  $i_{ld}$ ,  $i_{lq}$  and  $n_l$  to the RBF load point for comparison



# AC losses in dq Grid in SyMSpace

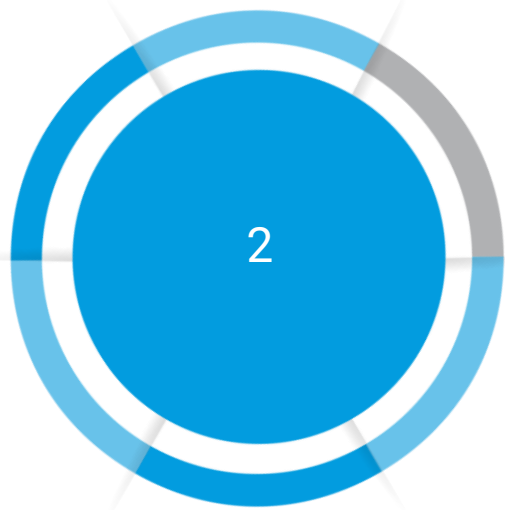
Add AC loss loadpoint to WebGUI project

The screenshot shows the SyMSpace Wizard interface with a search bar and a list of components. The component 'PMSM Loadpoint AClosses FEMM' is highlighted with a blue circle. Other components include 'ConstantLoad 0.1', 'PMSM Loadpoint EMForce 1.3', 'PMSM Loadpoint StatorStress FEMM 0.1-DEPRECATED', and 'PMSM MagnetLosses NGSolve 2.0'. The left sidebar shows a tree view of components, including 'M4UU-50A\_IsoVac', 'BMN-40SH/S\_Bomatec', 'Stress Boundary Condition', 'Optional', 'Optional Part', 'PMSM PMSM FEMM', 'PMSM\_Model\_RBF PMSM Model RBF', 'Postprocessing\_Settings PMSM Postprocessing Settings', 'LP\_NoLoad PMSM NoLoad RBF', and 'LP\_Nominal PMSM Loadpoint Motor RBF'.

Add Component „PMSM Loadpoint AClosses FEMM“ to a loadpoint

The screenshot shows the SyMSpace interface for the 'Loadpoint\_AClosses\_FEMM' component. It includes a 'Previews' section with four sub-views: 'Loadpoint', 'Loss Distribution', 'Loss Flow', and 'Power Flow'. The 'Parameters' section is expanded to show the 'Loss Distribution' parameters, which are displayed as a horizontal bar chart.

Component	Power / W
Pv	19.73 W
Pcu	7.25 W
Pcu_dc	7.06 W
Pcu_skin	0.03 mW
Pcu_proximity	2.25 mW
Pcu_strand	0.49 mW
Pcu_PWM	0.18 W
Pfe	11.89 W
Pfe_s_dc	1.71 W
Pfe_s_PWM	0.68 W
Pfe_r_dc	0.13 W
Pfe_r_PWM	0.59 W
Ppm	0.59 W
Ppm_eddy	0.59 W
Ppm_PWM	0.59 W
Ppw	0.59 W



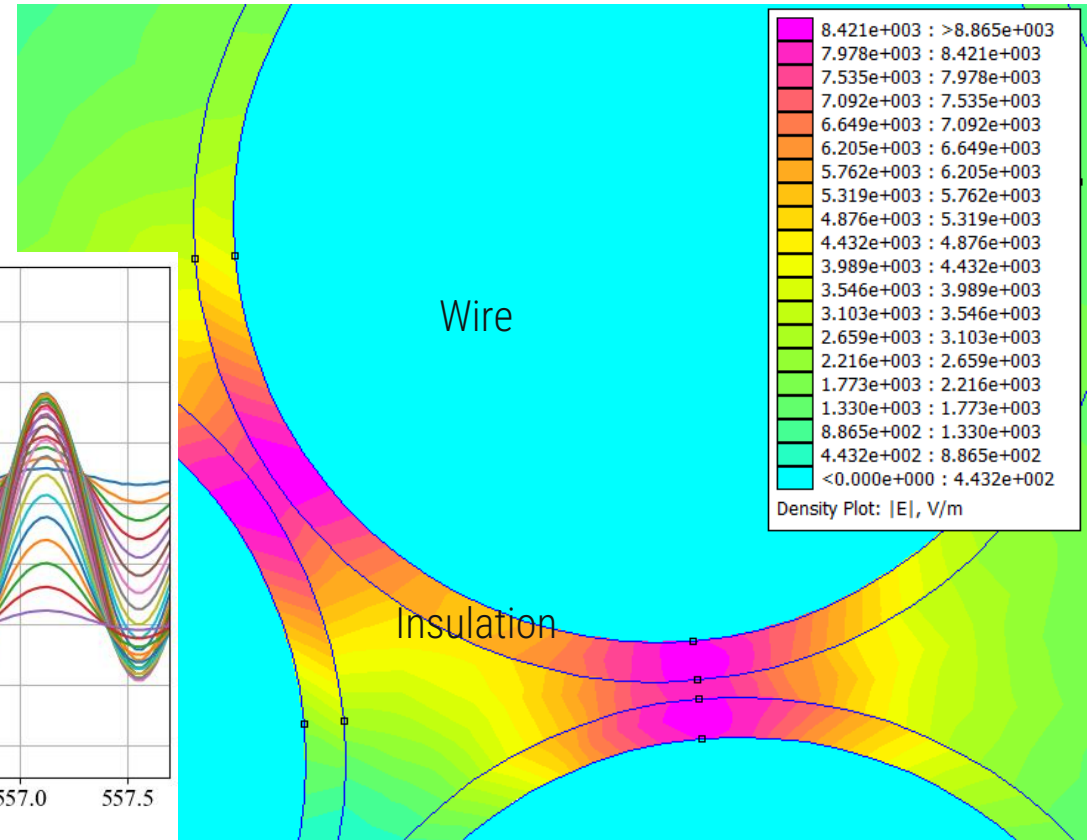
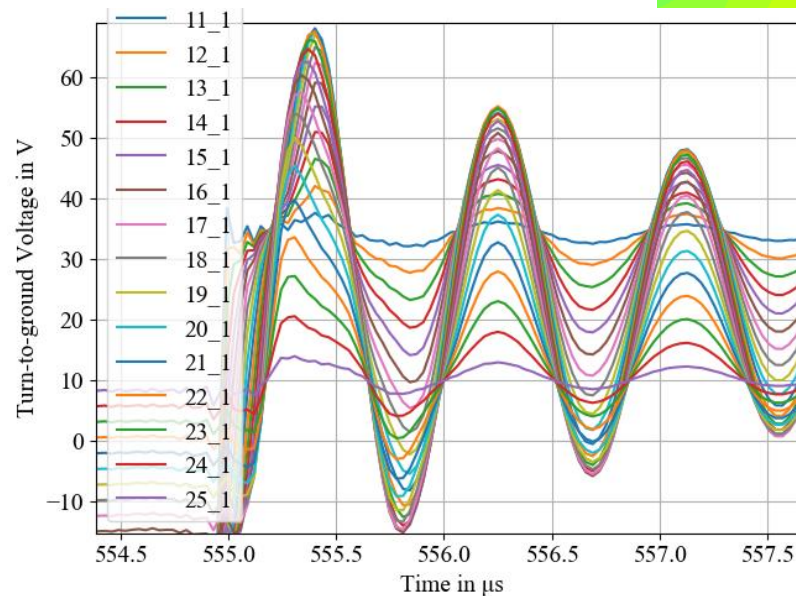
## Transient Voltage Effects



# Introduction

## Transient Voltage Effects in Electric Machines

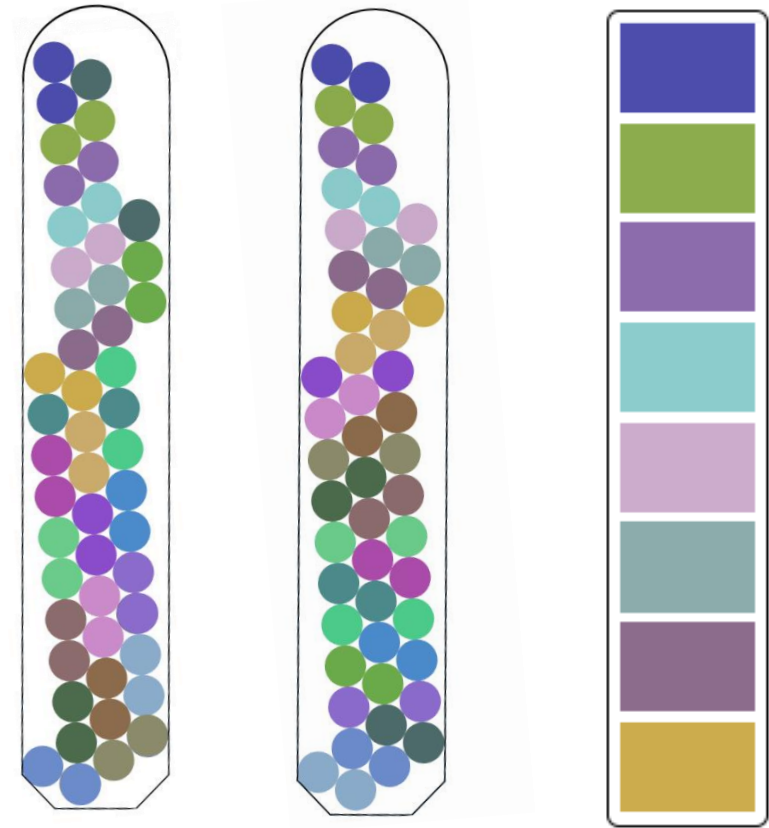
- Increasing switching frequencies and slew rates → electric stress on winding insulation in electric machines rises
- Distribution of voltage within winding is not uniform
- Transient overvoltages → damages in wire and slot insulation, partial discharge (PD)



# Introduction

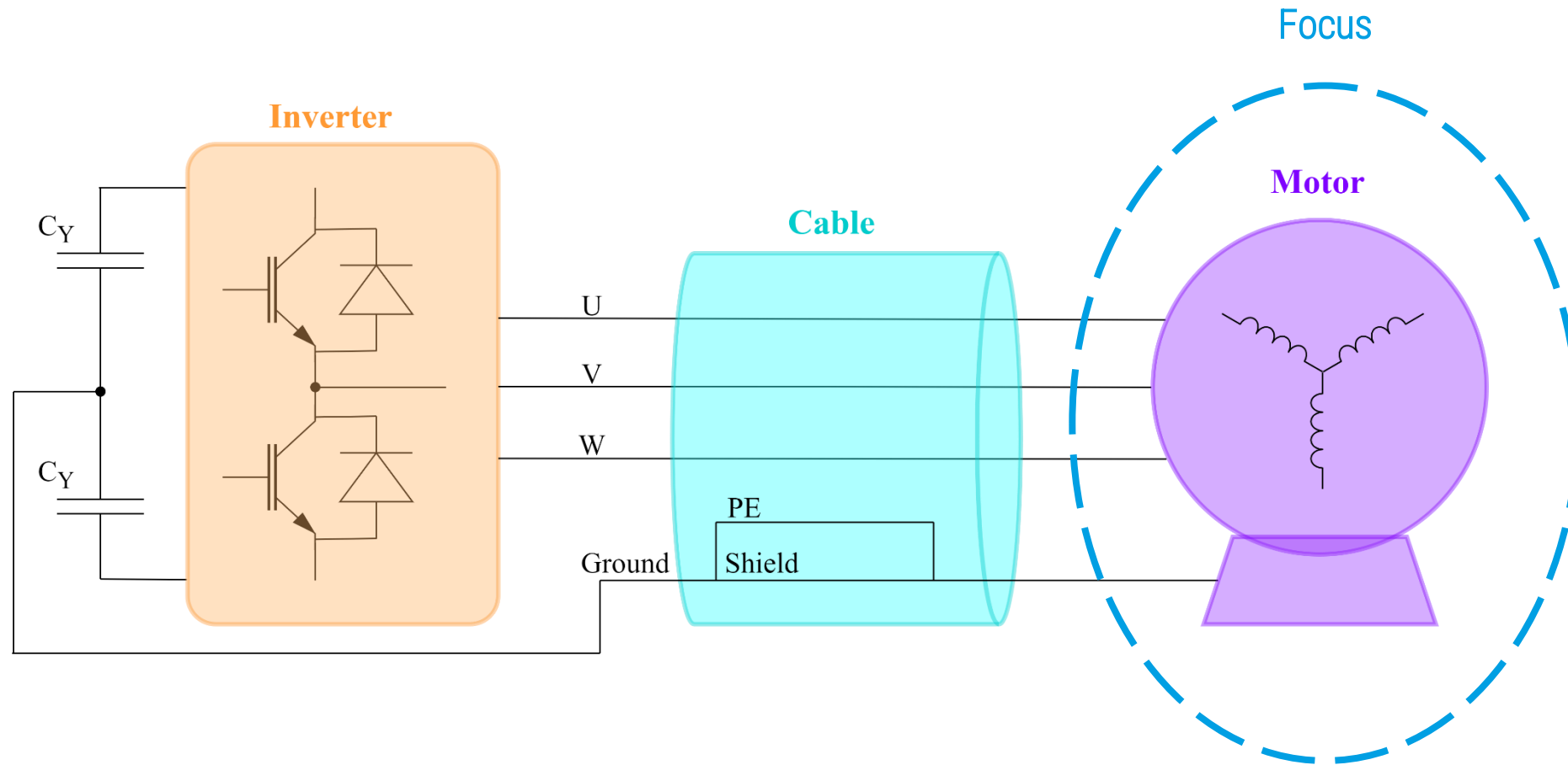
## Transient Voltage Effects in Electric Machines

- Insulation design → model for prediction of transient overvoltages necessary
- Random wound winding: position of wires not exactly known → worst case estimation
- Hairpin / form wound winding: position of wires well defined → voltage distribution can be calculated considering winding scheme



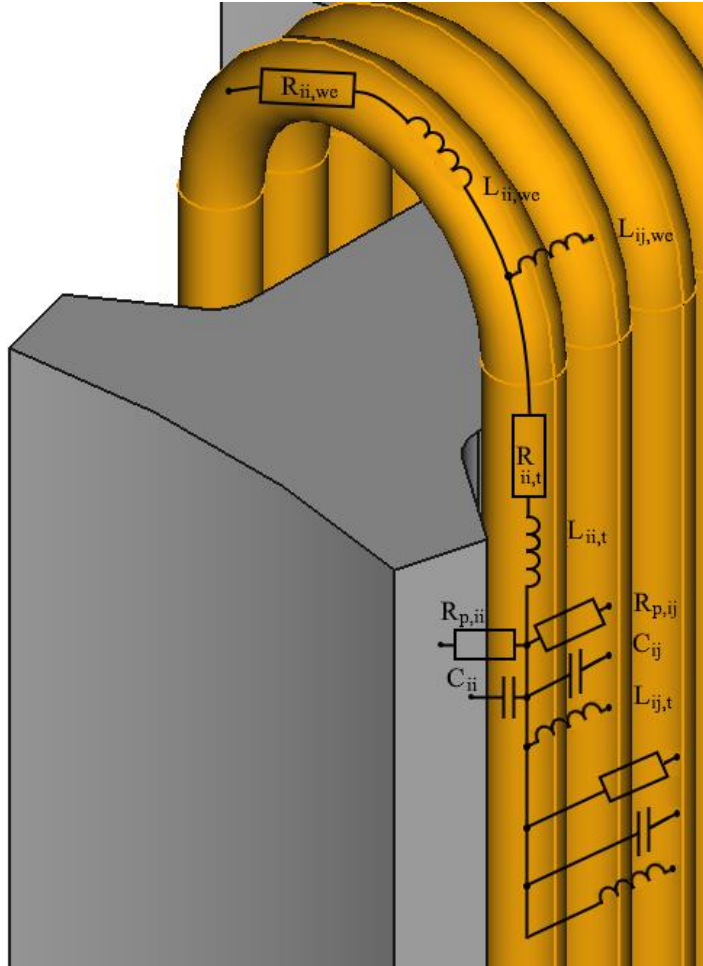
# Overall model

Inverter – Cable – Motor

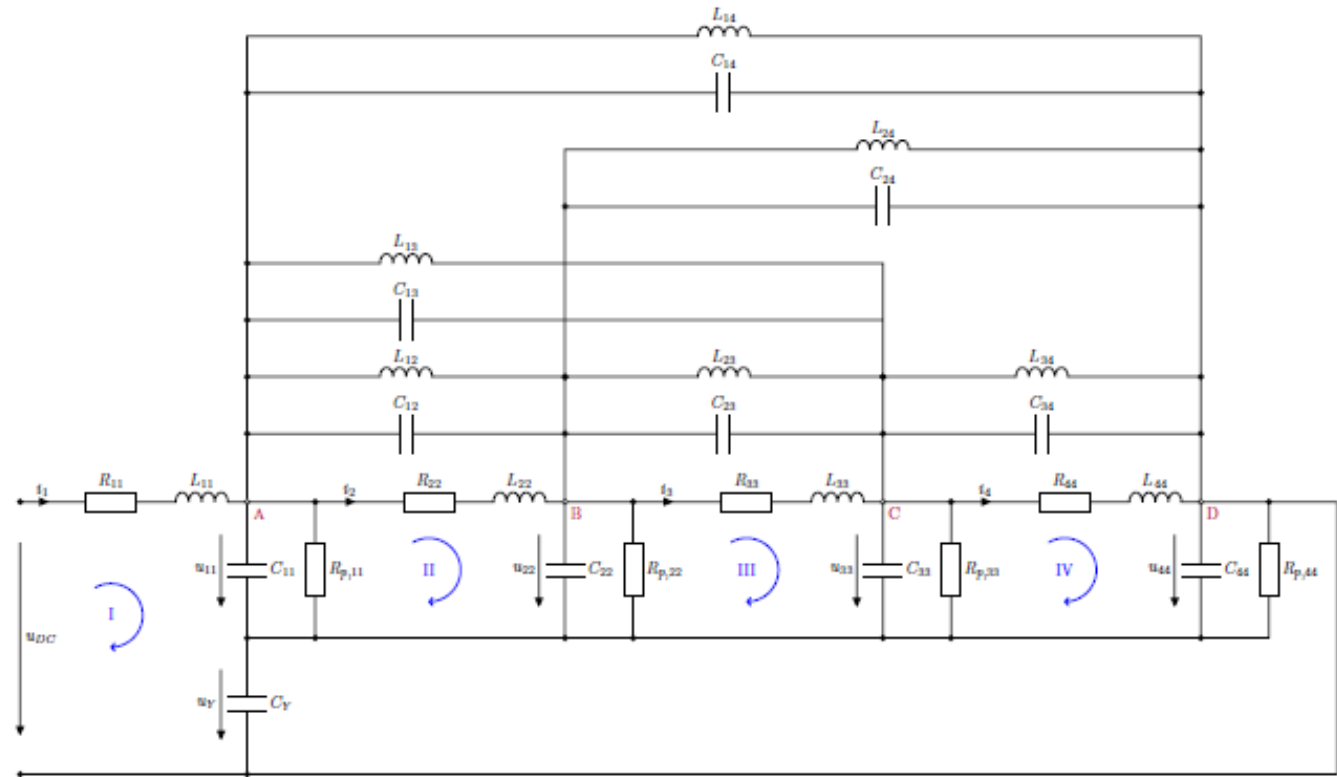


# Overview

## Model for transient voltage effects



- High-frequency motor model, evaluation of parameter in 2D FE or analytic
- Efficient computation in frequency domain → calculation of voltage overshoot

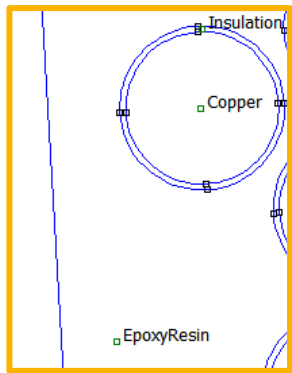


# Capacitance Matrix

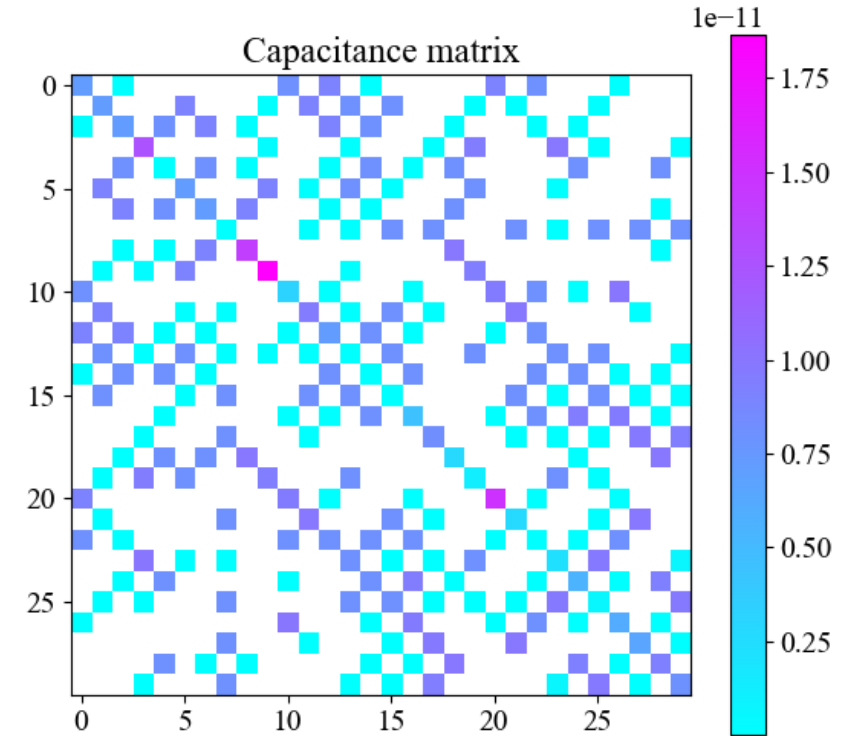
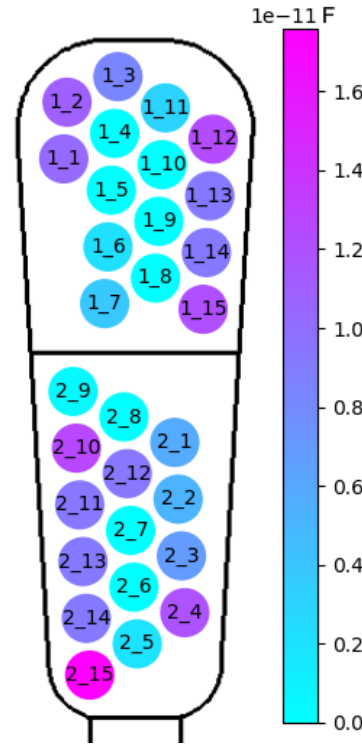
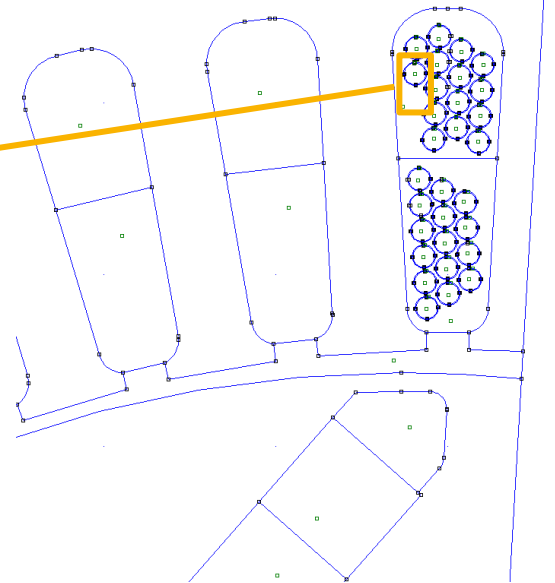
Simulation in FEMM electrostatic

Resulting capacitance values

- Main diagonal  $C_{ii}$ : Turn-to-ground capacitances
- Off diagonal  $C_{ij}$ : Turn-to-turn capacitances



Electrostatic FE model including insulation and epoxy resin

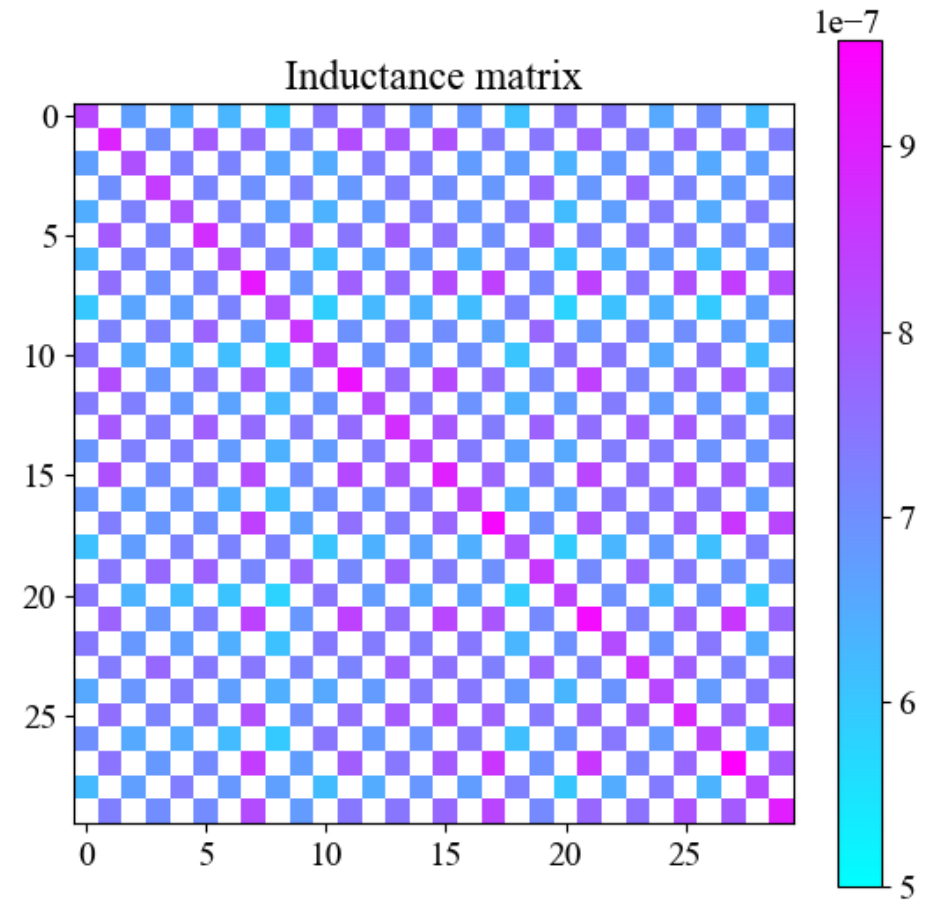
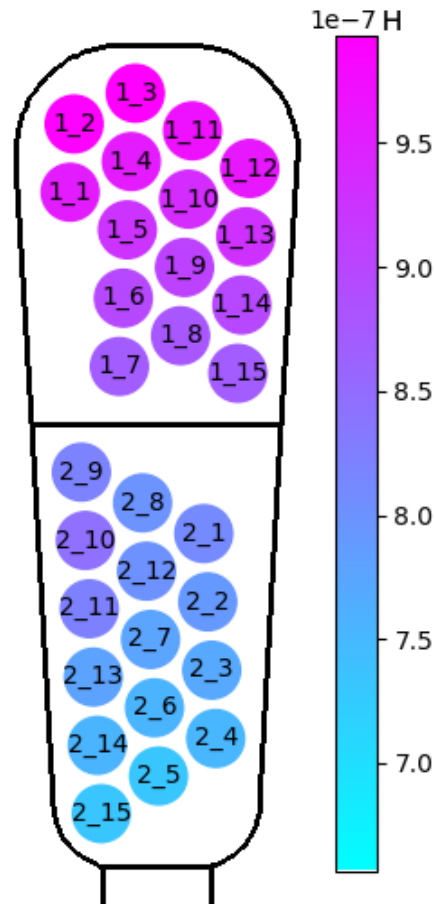


# Inductance Matrix

Simulation in FEMM Magnetostatic

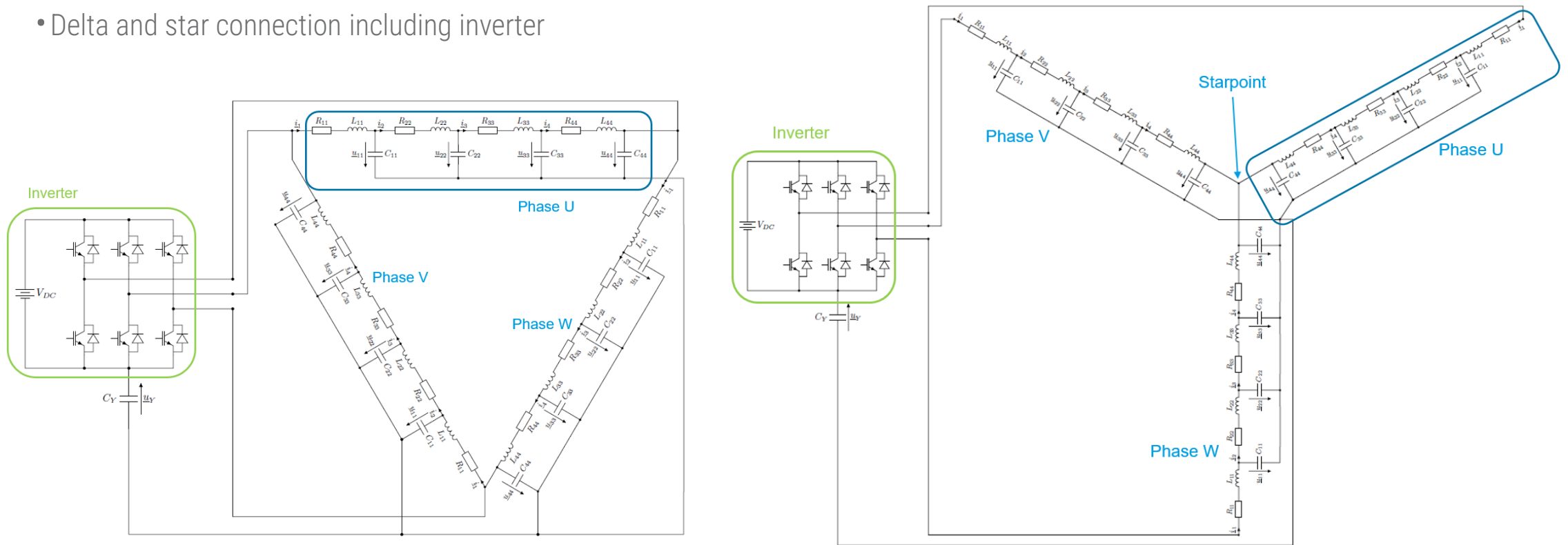
Resulting inductance values

- Main diagonal  $L_{ij}$ : Self inductances
- Off diagonal  $L_{ij}$ : Mutual inductances

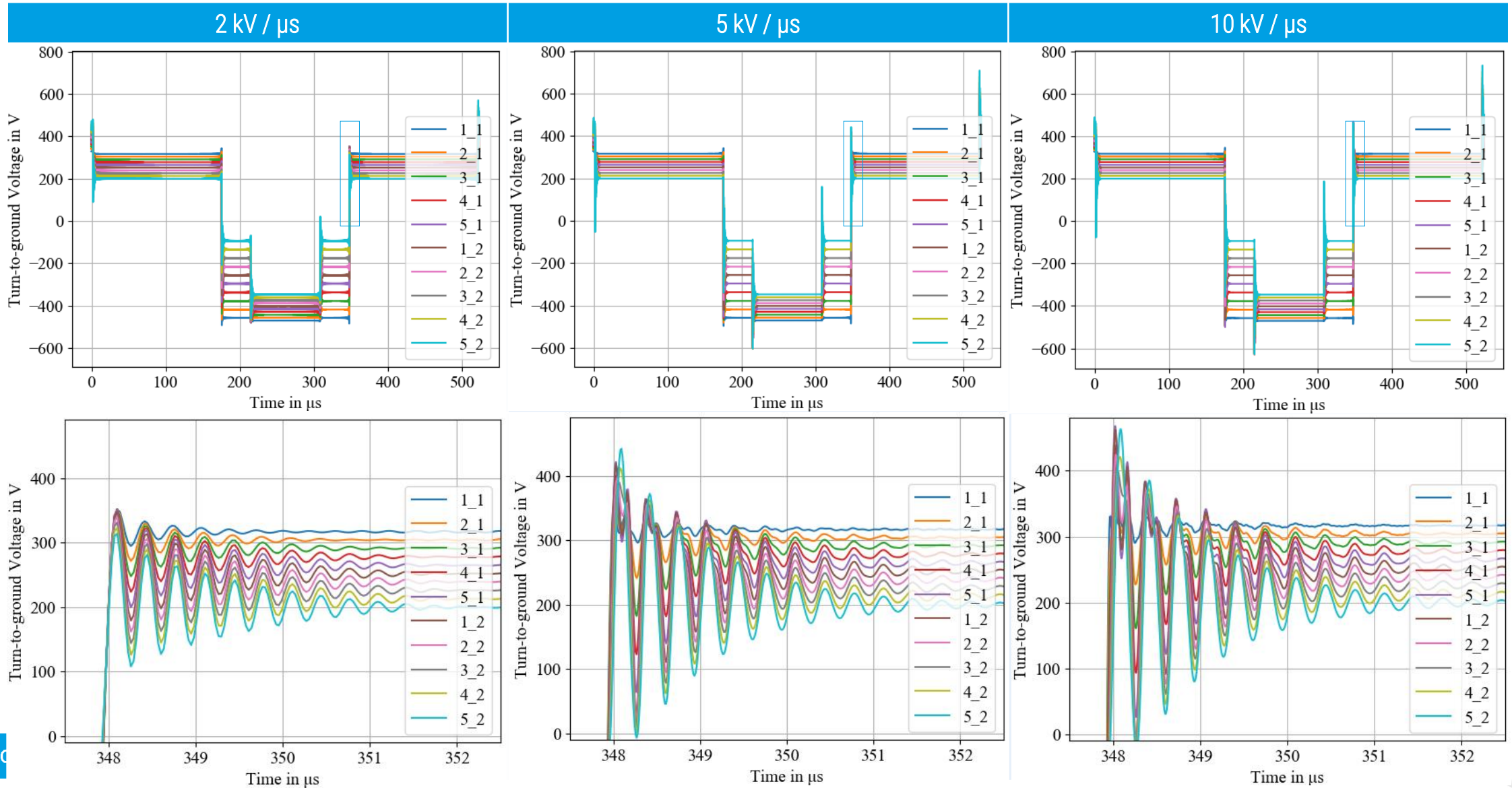


# Coil → Phase → Motor model

- Coils → Phase: winding scheme
- Delta and star connection including inverter



# Motor model – Turn-to-ground Voltage at different Slew Rates



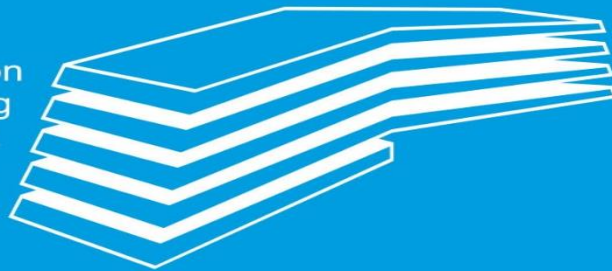


# Solution in the Frequency Domain

## Advantages

- Fast model evaluation, no time-consuming 3D or transient FEA
- Frequency dependency of parameters (resistances, inductances) - due to skin and eddy current effects - can be considered directly → higher accuracy, reduced number of network parameters compared to ladder network approximation
- Free software tools are used (Python, FEMM) → suitable for optimization

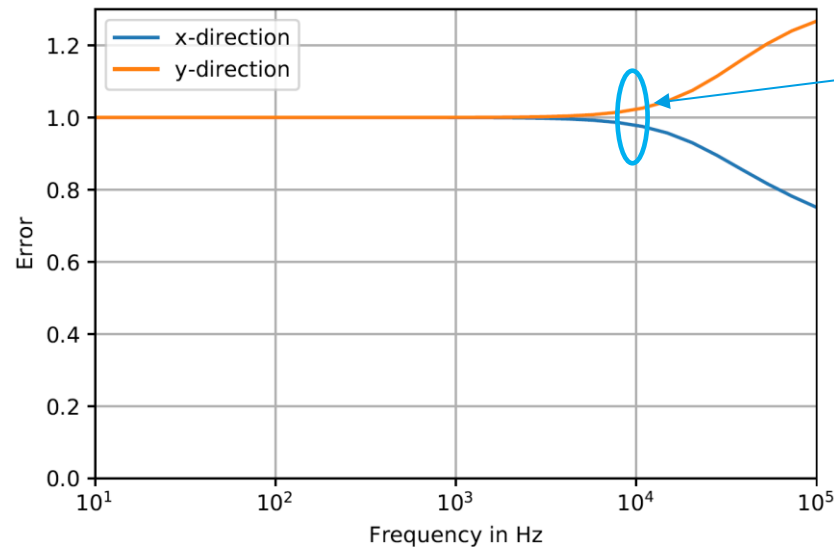
Customization  
Prototyping  
Development  
Research  
Science



# Proximity Losses

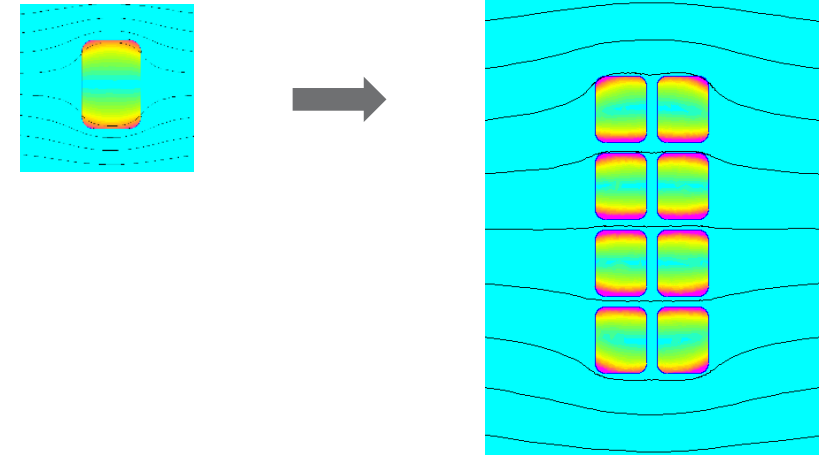
## Validation of losses

- Calculation method is based on single conductors.
- Is this method valid for a typical arrangement of conductors in the slot?



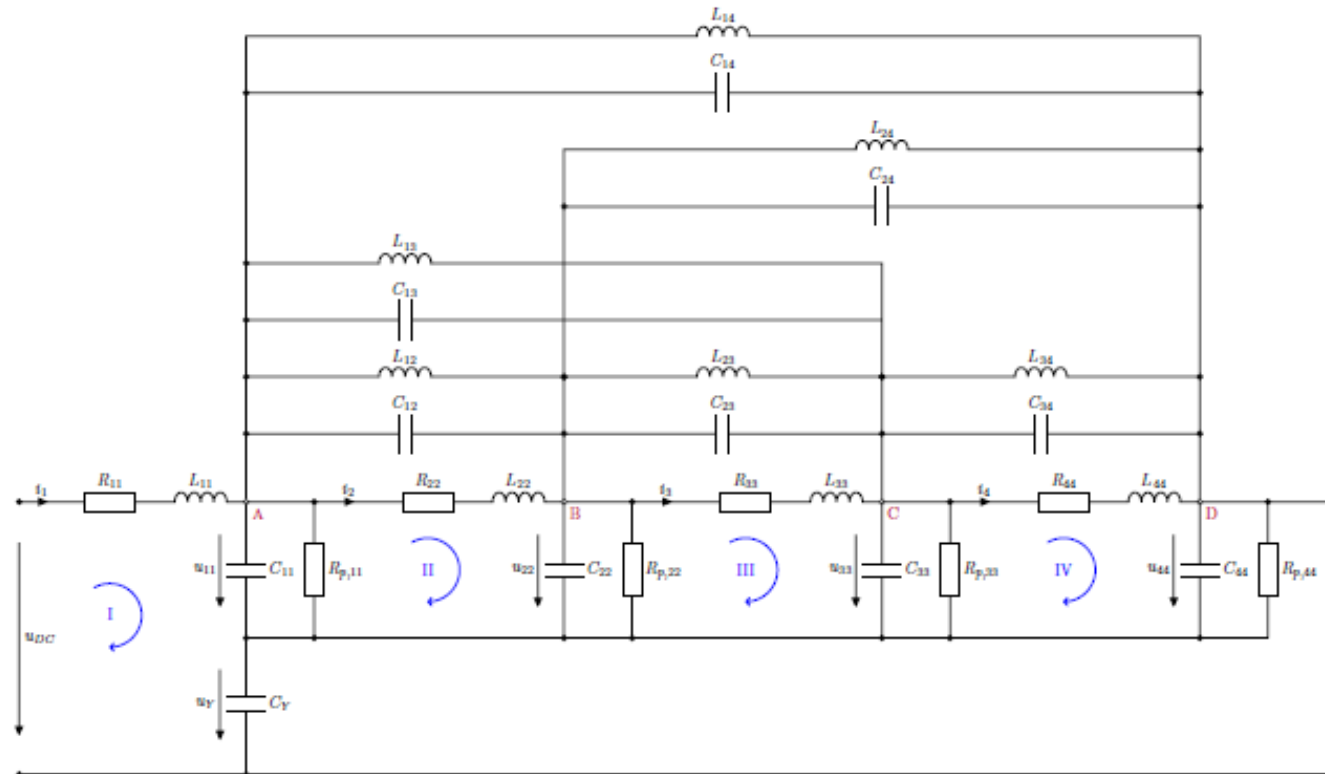
2.5% error at 10kHz

Error of the proximity losses for the array arrangement instead of single conductor



# Multi-Conductor Transmission Line Motor Model

## Network and equations



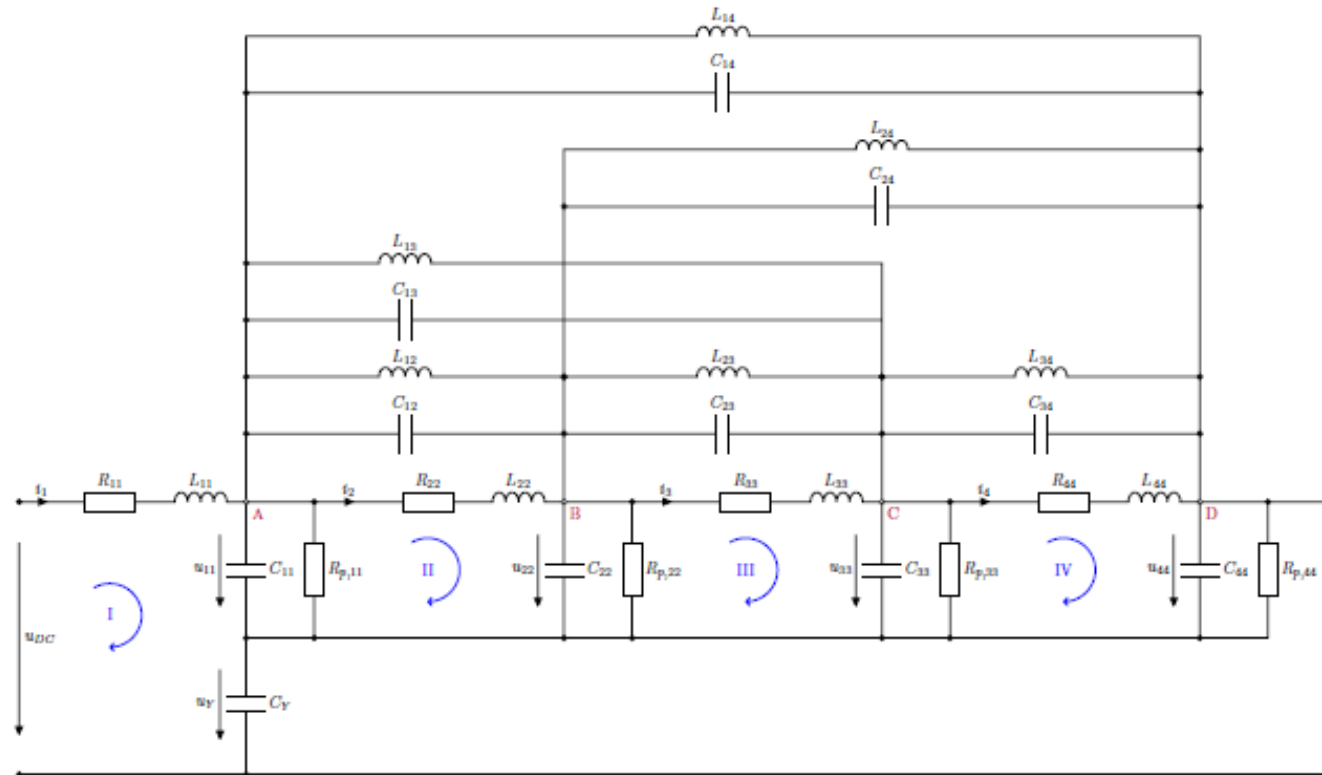
$$(A) \quad (C_{11} + C_{12} + C_{13} + C_{14}) \frac{du_{11}}{dt} - C_{12} \frac{du_{22}}{dt} - C_{13} \frac{du_{33}}{dt} - C_{14} \frac{du_{44}}{dt} = -\left(\frac{1}{R_{p,11}} + \frac{1}{R_{p,12}} + \frac{1}{R_{p,13}} + \frac{1}{R_{p,14}}\right)u_{11} + \frac{1}{R_{p,12}}u_{22} + \frac{1}{R_{p,13}}du_{33} + \frac{1}{R_{p,14}}u_{44} + i_1 - i_2$$

$$(B) \quad -C_{21} \frac{du_{11}}{dt} + (C_{21} + C_{22} + C_{23} + C_{24}) \frac{du_{22}}{dt} - C_{23} \frac{du_{33}}{dt} - C_{24} \frac{du_{44}}{dt} = \frac{1}{R_{p,21}}u_{11} - \left(\frac{1}{R_{p,21}} + \frac{1}{R_{p,22}} + \frac{1}{R_{p,23}} + \frac{1}{R_{p,24}}\right)u_{22} + \frac{1}{R_{p,23}}du_{33} + \frac{1}{R_{p,24}}u_{44} + i_2 - i_3$$

$$(C) \quad -C_{31} \frac{du_{11}}{dt} - C_{32} \frac{du_{22}}{dt} + (C_{31} + C_{32} + C_{33} + C_{34}) \frac{du_{33}}{dt} - C_{34} \frac{du_{44}}{dt} = \frac{1}{R_{p,31}}u_{11} + \frac{1}{R_{p,32}}du_{22} - \left(\frac{1}{R_{p,31}} + \frac{1}{R_{p,32}} + \frac{1}{R_{p,33}} + \frac{1}{R_{p,34}}\right)u_{33} + \frac{1}{R_{p,34}}u_{44} + i_3 - i_4$$

# Multi-Conductor Transmission Line Motor Model

State-space model



$$\bar{A} = \begin{pmatrix} -R_{11} & 0 & 0 & 0 & -1 & 0 & 0 & 1 \\ 0 & -R_{22} & 0 & 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & -R_{33} & 0 & 0 & 1 & -1 & 0 \\ 0 & 0 & 0 & -R_{44} & 0 & 0 & 1 & -1 \\ 1 & -1 & 0 & 0 & -\sum_{i=1}^4 \frac{1}{R_{p,1i}} & \frac{1}{R_{p,12}} & \frac{1}{R_{p,13}} & \frac{1}{R_{p,14}} \\ 0 & 1 & -1 & 0 & \frac{1}{R_{p,21}} & -\sum_{i=1}^4 \frac{1}{R_{p,2i}} & \frac{1}{R_{p,23}} & \frac{1}{R_{p,24}} \\ 0 & 0 & 1 & -1 & \frac{1}{R_{p,31}} & \frac{1}{R_{p,32}} & -\sum_{i=1}^4 \frac{1}{R_{p,3i}} & \frac{1}{R_{p,34}} \\ -1 & 0 & 0 & 1 & \frac{1}{R_{p,41}} & \frac{1}{R_{p,42}} & \frac{1}{R_{p,43}} & -\sum_{i=1}^4 \frac{1}{R_{p,4i}} \end{pmatrix}$$

$$\bar{B} = (1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0)^T$$

$$C = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ \vdots & & \ddots & & & & & \vdots \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$D = (0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0)^T$$

# Numerically Robust Solution of State-Space Model

$$F\dot{x} = \bar{A}x + \bar{B}u,$$

$$y = Cx + Du$$



~~$$A = F^{-1}\bar{A},$$

$$B = F^{-1}\bar{B}$$

$$\dot{x} = Ax + Bu,$$

$$y = Cx + Du$$~~

Matrix  $F$  has a very high condition number  
 → Inversion causes high numeric errors



Laplace transform

$$FX(s)s = \bar{A}X(s) + \bar{B}U(s),$$

$$Y(s) = CX(s) + DU(s)$$



$$X(s) = (Fs - \bar{A})^{-1}\bar{B}U(s),$$

$$Y(s) = CX(s) + DU(s).$$

$D = 0$



$$Y(s) = C(Fs - \bar{A})^{-1}\bar{B}U(s)$$

$$F = \begin{pmatrix} L_{11} & L_{21} & L_{31} & L_{41} & 0 & 0 & 0 & 0 \\ L_{12} & L_{22} & L_{32} & L_{42} & 0 & 0 & 0 & 0 \\ L_{13} & L_{23} & L_{33} & L_{43} & 0 & 0 & 0 & 0 \\ L_{14} & L_{24} & L_{34} & L_{44} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & \sum_{i=1}^4 C_{1i} & -C_{12} & -C_{13} & -C_{14} \\ 0 & 0 & 0 & 0 & -C_{21} & \sum_{i=1}^4 C_{2i} & -C_{23} & -C_{24} \\ 0 & 0 & 0 & 0 & -C_{31} & -C_{32} & \sum_{i=1}^4 C_{3i} & -C_{34} \\ 0 & 0 & 0 & 0 & -C_{41} & -C_{42} & -C_{43} & \sum_{i=1}^4 C_{4i} - C_Y \end{pmatrix}$$

$$\bar{A} = \begin{pmatrix} -R_{11} & 0 & 0 & 0 & -1 & 0 & 0 & 1 \\ 0 & -R_{22} & 0 & 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & -R_{33} & 0 & 0 & 1 & -1 & 0 \\ 0 & 0 & 0 & -R_{44} & 0 & 0 & 1 & -1 \\ 1 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & -1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\bar{B} = (1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0)^T$$

$$C = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ \vdots & & \ddots & & & & & \vdots \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$D = (0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0)^T$$